THE ORIGIN OF THE SURFACE FIELD ENHANCED COERCIVE FIELD IN
NANOPHASE Fe_{73.5}Cu_{1}Nb_{3}Si_{15.5}B_{7} RIBBON

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Dedicated to the memory of Professor Zvonko Ogorelec

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The influence of surface fields $H_p$ (generated with either direct or alternating
core-current) on soft magnetic properties of amorphous and nanocrystalline
Fe_{73.5}Cu_{1}Nb_{3}Si_{15.5}B_{7} ribbon has been studied. While in amorphous ribbon the co-
ceptive field $H_c$ decreases with $H_p$, in the same optimally annealed ribbon ($H_c = 1.3$
A/m, $M_m \approx M_s$) $H_c$ increases with $H_p$ and the hysteresis loss $E$ decreases with $H_p$
for all explored types of $H_p$ (static and dynamic with different phases with respect
to that of the magnetizing field $H$). The unexpected increase of $H_c$ in nanocrys-
talline ribbon is associated to the influence of $H_p$ on the surface and main (inner)
domain structure. The model is developed which takes into account this interaction
and explains all experimental results. The probable adverse effect of the external
fields with configurations similar to those of $H_p$ on the performance of such rib-
bons is briefly discussed and some procedures which can prevent these effects are
proposed.

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main structure, domain wall pinning, coercive field, core current

1. Introduction

The core-currents strongly affect the $M$–$H$ loops and hysteresis loss ($E$) of
amorphous ferromagnetic ribbons [1,2]. In particular, the direct current ($J_D$) may
decrease the coercive field $H_c$ (hence decrease $E$), shift the centre of the $M$–$H$
loop ($C$) along the $H$-axis, and change the permeability, maximum ($M_m$) and
remanant ($M_r$) magnetization of the sample [3]. Detailed investigations have shown
that these effects are associated with the perpendicular field $H_p$ generated by $J_D$
(static $H_p$). The magnitude of $H_p$ increases linearly with the distance $y$ from the
centre of the ribbon ($y = 0$) and reaches the maximum at the surface of the sample

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\( H_p = J_D y/w \), where \( w \) is the ribbon width and \(-t/2 \leq y \leq t/2\) is the perpendicular distance from the centre of the sample and \( t \) is the ribbon thickness \([2]\), hence the term “surface field”. Similar effects caused by the surface field \( H_p \) generated from external sources \([4]\) prove that \( H_p \) and not the core-current itself causes the observed effects. Later on it was found that \( H_p \) generated by alternating core-current \( J_A \) (dynamic \( H_p \)) decreases more efficiently \( H_c \) than the static \( H_p \) \([5]\).

In order to explain the observed effects and to help the understanding of the magnetization processes in soft ferromagnetic ribbons, a simple model for the influence of surface fields \( H_p \) on the magnetization of the sample consisting of two domains with antiparallel domain magnetization \( I \) has been developed \([6]\). This model, in addition to the explanation of the changes in the \( M-H \) loop caused by \( H_p \), also provides a qualitative (sometimes quantitative) insight into the domain wall (DW) pinning, domain structure and the magnetic anisotropy. For the coercive field model predicts a linear decrease of \( H_c \) with \( H_p \) (at not too small \( H_p \)) provided that \( I \) forms an angle with the ribbon axis. The measurements of \( H_c \) vs. \( H_p \) for a number of amorphous ferromagnetic ribbons (both magnetostrictive and nonmagnetostrictive) agreed well with the model prediction for moderate values of static \( H_p \), whereas at elevated surface fields \( H_p \), the decrease of \( H_c \) with \( H_p \) slows down and \( H_c \) tends to saturation \([3]\). The effects of dynamic \( H_p \) on \( H_c \) were qualitatively the same as for the static \( H_p \), but in several samples (in which the difference in DW pinning strengths at opposite surfaces was sufficiently large) the decrease of \( H_c \) with increasing \( H_p \), continued until \( H_c = 0 \) was reached \([5]\). The observed deviations from the model predictions at elevated surface fields \( H_p \) were ascribed to the complex domain structure of real sample and the influence of high surface field on this structure, but these ingredients have not been incorporated in the model.

However, recent results show \([7]\) that \( H_c \) of nanocrystalline \( \text{Fe}_{73.5}\text{Cu}_{1.5}\text{Nb}_{3}\text{Si}_{15.5}\text{B}_{7} \) ribbon (hereafter \( \text{FeCuNbSiB} \)) increases with \( H_p \) (whereas loss \( E \) decreases with \( H_p \)) which is at variance with the predictions of simple model for the influence of \( H_p \) on the \( M-H \) loops of ferromagnetic ribbons. These results call for the revision of the model which should take into account the influence of the surface field on the actual domain structure (DS) and the DW pinning associated with the surface DS (SDS). Here, in addition to the description of the ‘unusual’ influence of \( H_p \) (both static and dynamic) on the \( M-H \) loops and their parameters for nanocrystalline \( \text{FeCuNbSiB} \) ribbon, we also present the improved model which fully accounts for the observed phenomena. This model yields a better insight into the magnetization processes in the soft ferromagnetic ribbons and may also help to find the methods for the improvement of their soft magnetic properties.

2. Experimental procedures

The amorphous \( \text{FeCuNbSiB} \) ribbon with dimensions \( l \times w \times t = 200 \times 2 \times 0.02 \) mm\(^3\) was prepared by the melt-spinning technique in Vacuumschmelze GmbH, Hanau, Germany. After the magnetization measurements of the as-prepared sample, the same ribbon was brought into the nanocrystalline state by thermal an-
nealing at $T_a = 540^\circ$ C for one hour. The annealing was performed in a long tube furnace in the atmosphere of pure argon gas. The magnetization measurements were performed with an induction technique at room temperature [8]. In all magnetization measurements we used triangular magnetizing field $H(t)$ at the frequency $f = 5.5$ Hz. For the measurement of $H_c$ and $M_t$ as a function of $M_m/M_s$ ($M_s$ is the saturation magnetization) we varied the amplitude $H_0$ of the magnetizing field ($H_0 \leq 350$ A/m). The investigation of the influence of the static and dynamic $H_p$ on the $M$–$H$ loops and their parameters ($H_c$, $C$, $M_m$, $M_r$, $\mu_{\text{max}}$) was performed at fixed amplitudes of $H$ ($H_0 = 100$ A/m and 10 A/m). The static and dynamic surface fields $H_p$ were achieved with either direct ($J_D \leq 100$ mA) or alternating current ($J_A = J_{A0} \sin \omega t$, with $J_{A0} \leq 110$ mA and $\omega = 2\pi f = 11\pi/s$) flowing along the ribbon. The magnetizing field $H$ and the alternating core-current $J_A$ were synchronized with the phase of $J_A$ shifted for either $\pi/2$ (inset to Fig. 1) or $3\pi/2$ in respect to that of $H$. Some data relevant to our FeCuNbSiB sample (both for amorphous and nanocrystalline state) are given in Table 1.

![Fig. 1. Schematic drawing of the domain wall DW, domain magnetizations $I$, magnetizing field $H$ and surface fields $H_p$ generated by the core current $J_D$. The inset: drive field (dotted) alternating core current relationship.](image)

**TABLE 1.** Data relevant to Fe$_{73.5}$Cu$_{11}$Nb$_{3}$Si$_{15.5}$B$_{7}$ sample before annealing and after annealing at $T_a = 540^\circ$ C: $H_{c0}$, $M_m/M_s$ and $\mu_{\text{max}}$ are the coercive field, normalized maximum magnetization and maximum permeability, respectively, in the absence of surface fields. $\langle \delta \rangle$ is the average angle between the magnetization of the domains and the ribbon axis deduced from the variations of the $H_c$ and $C$ with the static surface field $H_p$. A triangular drive field $H$ with the amplitude $H_0 = 100$ A/m and frequency $f = 5.5$ Hz was used.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$H_{c0}$ (A/m)</th>
<th>$M_m/M_s$</th>
<th>$\langle \delta \rangle$ (°)</th>
<th>$\mu_{\text{max}}$ (Tm/A)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prean.</td>
<td>13.5</td>
<td>0.40</td>
<td>2.4</td>
<td>$9.7 \times 10^4$</td>
</tr>
<tr>
<td>After an.</td>
<td>1.3</td>
<td>0.96</td>
<td>2.5</td>
<td>$9.8 \times 10^4$</td>
</tr>
</tbody>
</table>
3. The model

The model we propose is based on the following common characteristics of the soft ferromagnetic samples in the shape of long ribbon:

- The domain structure has usually two components: the main (inner) domain structure (MDS) which consists of rather wide domains separated with 180°-DWs and dominates the magnetization of the ribbon along its axis [9], and the surface domain structure (SDS) consisting of fine domains forming a complex patterns associated with the closure of the magnetizations of MDS, local magnetic anisotropy and the surface inhomogeneities [10].

- The magnetizations of the domains \( I \) of the MDS form nonzero angle \( \delta \) with the ribbon axis and this angle is not the same for all domains of MDS [11].

- Because of usually small angles \( \delta \), the magnetization of the ribbons in moderate fields along the axis (such as those used in present measurements) proceeds usually via the motion of 180°-DWs of MDS [12,13].

- Usually the strongest pinning centres for DWs of MDS are located in the vicinity of the surfaces of the sample and their strengths are usually different at the opposite surfaces [14].

- These surface pinning centres are associated with the surface inhomogeneities, stresses and irregularities/roughness (intrinsic pinning), and also with some domains from SDS, whose magnetizations form large angles \( \delta \) with the ribbon axis (SDS pinning) [15].

For simplicity, we consider the motion of one 180°-DW separating two domains from MDS with antiparallel \( I \)s (Fig. 1). In order to account for more complex MDS of real ribbon, we denote the angle between the domain magnetizations and ribbon axis with \( \langle \delta \rangle \), which could be regarded as an average value of \( \delta \) corresponding to MDS domains participating in the magnetization processes for given magnetizing field amplitude \( H_0 \). The magnitudes of \( H \) necessary for depinning of DWs at the upper and lower surface of the ribbon (in the absence of the surface field \( H_p \)) we denote as \( H_{su0} \) and \( H_{sl0} \), respectively, (subscript 0 denotes \( H_p = 0 \)). Since usually \( H_{su0} \neq H_{sl0} \), we assume \( H_{su0} < H_{sl0} \) [14]. Therefore, in the absence of \( H_p \), \( H_c = H_{su0} \equiv H_{sl0} \). When \( J_D \) flows along the sample during the magnetization cycle, the generated surface field \( H_p \) (Fig. 1) has the projection \( P = H_p \sin(\langle \delta \rangle) \) on \( I \), which together with the projection of the magnetizing field \( H \cos(\langle \delta \rangle) \) contributes to the pressure on DW. Accordingly, the magnitude of the magnetizing field \( H \) necessary for depinning of DW at the upper or lower surface of the ribbon may increase or decrease with respect to \( H_{su0} \) or \( H_{sl0} \) depending on the direction of \( J_D \). (This was the essence of the earlier model which ignored SDS [6].)

However, in a real sample there is an interplay between MDS and SDS and this interaction is affected by the surface field. In particular, the surface domains, which form large angles with the ribbon axis, can act as the pinning centres for DWs of
MDS [15]. Clearly, this SDS type of DW pinning is enhanced with \( H_p \) which tends to fix and/or rotate the magnetizations of such domains. Therefore, the magnitude of the magnetizing field \( H \) necessary for depinning of DWs belonging to MDS will be enhanced and this enhancement will depend on the magnitude of \( H_p \). This enhancement can be different at the opposite surfaces of the sample and its actual dependence on \( H_p \) is not known to us. However, in a case of moderate \( H_p \) it is reasonable to assume a linear variation of the SDS pinning with \( H_p \). Therefore, we assume (and the experimental results for FeCuNbSiB ribbon seem to confirm) that the DW pinning enhancement due to SDS is equal for upper and lower surface of the ribbon and is proportional to \( \frac{H_p}{2} \), i.e. equal to \( kH_p \) (where \( k \) is the proportionality constant which depends on the SDS of the given sample).

Since we wish to model the dynamic \( M-H \) loops, we denote the magnitudes of the magnetizing field necessary for the depinning of DW belonging to MDS at the upper and lower surface of the sample in the presence of \( J_D \) with \( H_{su} \) and \( H_{sl} \), respectively, when the magnetizing field increases from \(-H_0\) to \( H_0 \) and the corresponding symbols for the reverse part of the cycle (from \( H_0 \) to \(-H_0\)) are \( H_{su}^- \) and \( H_{sl}^- \). Accordingly, the expressions for the depinning fields in the presence of \( J_D \) are

\[
\begin{align*}
H_{su} &= H_{su0} + kH_p \mp H_p \tan(\langle \delta \rangle), \\
H_{sl} &= H_{sl0} + kH_p \pm H_p \tan(\langle \delta \rangle), \\
H_{su}^- &= -(H_{su0} + kH_p) \mp H_p \tan(\langle \delta \rangle), \\
H_{sl}^- &= -(H_{sl0} + kH_p) \pm H_p \tan(\langle \delta \rangle).
\end{align*}
\]

The upper signs in Eqs. (1)–(4) correspond to \( J_D \) direction as shown in Fig. 1, whereas the lower signs correspond to the opposite direction of \( J_D \). Since the magnetization of the sample changes as soon as the magnetizing field \( H \) reaches the lower value of the two values necessary for the depinning of DW from the upper and lower surface of the sample, in a given condition, only a part of Eqs. (1)–(4) will be relevant for the determination of the width (\( H_c \)) and the position of the centre (\( C \)) of the \( M-H \) loop. Accordingly, when the strength of pinning of DWs at the opposite surface of the ribbon is a different, one has two different situations depending on \( H_p \geq \mid H_{su0} \mid \) or \( \leq (H_{sl0} - H_{su0})/(2 \tan(\langle \delta \rangle)) \). In a case A) when \( H_p \leq (H_{sl0} - H_{su0})/(2 \tan(\langle \delta \rangle)) \), \( |H_{su}| < |H_{sl}| \) and \( |H_{su}^-| < |H_{sl}^-| \) is fulfilled for both directions of \( J_D \), one finds

\[
H_c = \frac{1}{2} (H_{su} - H_{su}^-) = H_{co} + kH_p \tag{5}
\]

and

\[
C = \frac{1}{2} (H_{su} + H_{su}^-) = \mp H_p \tan(\langle \delta \rangle). \tag{6}
\]

According to Eqs. (5) and (6), the coercive field increases with \( H_p \) when SDS pinning is present, whereas the centre \( C \) of the \( M-H \) loop shifts with \( H_p \) in either
negative or positive direction along the $H$-axis, depending on the direction of $J_D$. The shift $C$ depends on angle $\langle \delta \rangle$ but not on SDS pinning since $kH_p$ terms cancel in Eq. (6).

For $H_p \geq (H_{sl0} - H_{su0})/(2 \tan(\delta))$, regime B, is $|H_{su}| < |H_{sl}|$ and $|H_{su}^-| < |H_{sl}^-|$ for the direction of $J_D$ as in Fig. 1, whereas for the opposite direction of $J_D$, $|H_{su}| < |H_{sl}|$ and $|H_{su}^-| < |H_{sl}^-|$ is fulfilled. The calculations analogous to those performed in a case A yield for both directions of $J_D$

$$H_c = \frac{1}{2} (H_{su0} + H_{sl0}) + kH_p - H_p \tan(\delta)$$

and

$$C = \pm \frac{1}{2} (H_{sl0} - H_{su0}).$$

In this range of $H_p$, the coercive field (Eq. (7)) may either increase or decrease with $H_p$ depending on $k > \tan(\delta)$, i.e. whether the enhancement of SDS pinning or a pressure of $H_p$ on DWs prevails. In a special case $k = \tan(\delta)$, $H_c$ would remain constant at the magnitude reached at the end of regime A (Eq. (5)). The position of the centre of the $M$–$H$ loop should be fixed (Eq. (8)) at the maximum value reached in regime A (Eq. (6)), providing that the enhancement of the SDS pinning at both surfaces of the sample is the same.

Next we briefly describe the influence of dynamic $H_p$ with the amplitude $H_{p0}$ on $H_c$ and $C$. The calculation is simplified [5] by assuming that the alternating core current $J_A$ has the square waveform and the same frequency as $H$, but with phase adjusted with respect of that for $H$ as illustrated in the inset to Fig. 1 (synchronization suitable for the decrease of $H_c$, hence suitable phase). In that case one obtains the relations for the depinning fields $H_i$ ($i = u, l$) from Eqs. (1)–(4) by taking into account the change in the direction of $J_A$ during the magnetization cycle ($J_A$ has opposite directions for the increasing ($-H_0 \rightarrow H_0$) and decreasing ($H_0 \rightarrow -H_0$) branch of the $M$–$H$ loop, respectively)

$$H_{su} = H_{su0} + kH_{p0} - H_{p0} \tan(\delta),$$

$$H_{sl} = H_{sl0} + kH_{p0} + H_{p0} \tan(\delta),$$

$$H_{su}^- = -(H_{su0} + kH_{p0}) + H_{p0} \tan(\delta),$$

$$H_{sl}^- = -(H_{sl0} + kH_{p0}) - H_{p0} \tan(\delta).$$

Equations (9)–(12) show that $|H_{su}| < |H_{sl}|$ and $|H_{su}^-| < |H_{sl}^-|$ irrespective of the amplitude of the surface field $H_{p0}$. Accordingly,

$$H_c = H_{c0} + kH_{p0} - H_{p0} \tan(\delta)$$

should be fulfilled for any value of $H_{p0}$. The variation of $H_c$ with $H_{p0}$ depends on $k > \tan(\delta)$ similarly to the case described by Eq. (7). The centre of the $M$–$H$ loop is unshifted ($C = 0$, Eqs. (9) and (11)).
Further shift of the phase of $J_A$ with respect to that of $H$ for additional 180° (unsuitable phase, causes an increase of $H_c$ with $H_{p0}$ [6]) leads to the expressions for the depinning fields $H_{si}$ which are formally the same as Eqs. (9) – (12) but have opposite signs in front of $H_{p0} \tan(\delta)$ terms. However, in this case depending on the magnitude of $H_{p0}$, two regimes (analogous to those in the case of $J_D$) with different variations of $H_c$ appear

A) for $H_{p0} \leq (H_{s0} - H_{su0})/2 \tan(\delta)$ follows $|H_{su}| < |H_{si}|$ and $|H_{su}^-| < |H_{si}^-|$ with

$$H_c = H_{s0} + kH_{p0} + H_{p0} \tan(\delta),$$

which means that $H_c$ increases with $H_{p0}$ irrespective of $k > 0$ or $\tan(\delta)$, i.e. the broadening of $M$–$H$ loop with $H_{p0}$ is further enhanced by the SDS pinning. 

B) for $H_{p0} \geq (H_{s0} - H_{su0})/2 \tan(\delta)$ $|H_{su}| < |H_{si}|$ and $|H_{su}^-| < |H_{su}^-| \text{ is fulfilled}$, hence,

$$H_c = H_{s0} + kH_{p0} - H_{p0} \tan(\delta),$$

i.e. the variation of $H_c$ with $H_{p0}$ depends on $k > 0$ or $\tan(\delta)$ as was the case in Eq. (7). In both regimes the position of the centre of the $M$–$H$ loop does not depend on $H_{p0}$, i.e. $C = 0$ is fulfilled.

The above expresions are derived for the square wave form of $H_{p0}$ ($J_A$), whereas in the experiments we used sinusoidal $J_A$. However, the earlier experiments have shown that the effect of sinusoidal $H_p$ is practically the same as that of square wave one [5] and the sinusoidal $J_A$ results in less noise in the magnetization measurements.

Although the above model for the influence of $H_p$ on the SDS pinning of DWs belonging to MDS is quite general, in the derivation of specific results for $H_c$ and $C$ we used two simplifying assumptions: (i) the enhancement of SDS pinning is proportional to $H_{p0}$ ($kH_p$ or $kH_{p0}$), (ii) this enhancement is the same at both surfaces of the sample ($k_u = k_l \equiv k$). The validity of these assumptions has to be verified by experiment.

4. Results and discussion

The amorphous FeCuNbSiB ribbons show poor soft magnetic properties due to the very strong local magnetic anisotropy (induced during the production of this magnetostrictive ferromagnet) and the associated strong volume pinning centres for DWs [16]. Our measurements performed prior to thermal annealing confirm these findings (Table 1). Due to the strong volume pinning of DWs belonging to MDS for $H_0 = 100 \text{ A/m}$, the coercive field is quite large (13.5 A/m) and the ratio $M_m/M_s$ quite small (0.4). The slope of log $H_c$ vs. log($M_m/M_s$) variation (Fig. 2) is approximately constant within the explored range of $M_m$ ($M_m/M_s \leq 0.5$ for $H_0 \leq 350 \text{ A/m}$). Since the strength of DW pinning is proportional to this slope [17], the unique slope indicates that one type of pinning centres dominates the magnetization processes in amorphous FeCuNbSiB ribbons for $M_m/M_s \leq 0.5$. 

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Fig. 2. Variation of the coercive field $H_c$ (a) and remanent magnetization $M_r$ (b) with the normalized magnetization $M_m/M_s$ before annealing (open symbols) and after annealing at temperature $T_a = 540^\circ$ C (solid symbols) for the Fe$_{73.5}$Cu$_1$Nb$_{3.5}$Si$_{15.5}$B$_7$ ribbon. A triangular drive field $H$ with the frequency $f = 5.5$ Hz and different amplitudes $H_0 \leq 350$ A/m was used.

Simultaneously, the remanent magnetization tends to saturate for $M_m/M_s > 0.3$ (Fig. 2b). This is consistent with strong volume pinning which inhibits the motion of DWs (since $M_m/M_s \leq 0.5$ only a fraction $\leq 50\%$ of MDS participates in the magnetization of the sample along its axis) and the magnetization processes for $M_m/M_s > 0.3$ possibly proceed via bulging of the free parts of DWs situated between strong pinning centres [17]. Since DW bulging is reversible process, $M_r$ saturates.

Under such conditions, the influence of static surface field on the parameters of the $M$–$H$ loops is weak. Indeed, for $H_0 = 100$ A/m, $H_c$ decreases approximately linearly with $H_p$ (Fig. 3) for $H_p \geq 5$ A/m, in agreement with Eq. (7) for $k < \tan(\delta)$, but the relative decrease is quite small ($\Delta H_c/H_{c0} \approx 0.1$ for $H_p = 24$ A/m) and the changes of $M_m$ and $C$ with $H_p$ are slight. This occurs because $H_p$ has the largest magnitude at the surfaces of the sample ($H_p = J_D/2w$) and therefore exerts little influence on strong volume pinning centres (located in the interior of the sample where $H_p \to 0$). Accordingly, the intrinsic surface pinning and SDS pinning have little influence on magnetization processes in as-prepared amorphous FeCuNbSiB ribbons.

In order to check whether this conclusion depends on the magnitude of $H_0$ (hence the value of $M_m$) or not, we also measured the influence of static $H_p$ on the parameters of the $M$–$H$ loop for $H_0 = 25$ A/m ($M_m \approx 0.26 M_s$). As seen from Fig. 4, the variations of $H_c$, $M_m$ and $C$ with $H_p$ for $H_0 = 25$ A/m are essentially the same as those for $H_0 = 100$ A/m (Fig. 3). In particular, for $|H_p| > 5$ A/m, $H_c$
Fig. 3. Variation of the coercive field $H_c$ (■), maximum magnetization $\mu_0 M_m$ (△) and the position of the centre of the $M-H$ loop $C$ (□) with the magnitude of static surface field $H_p$ for the Fe$^{73.5}$Cu$^{11}$Nb$^3$Si$^{15.5}$B$^7$ ribbon in the amorphous state. A triangular drive field $H$ with the frequency $f = 5.5$ Hz and the amplitude $H_0 = 100$ A/m was used.

Fig. 4. Variation of the coercive field $H_c$ (■), maximum magnetization $\mu_0 M_m$ (△) and the position of the centre of the $M-H$ loop $C$ (□) with the magnitude of static surface field $H_p$ for the Fe$^{73.5}$Cu$^{11}$Nb$^3$Si$^{15.5}$B$^7$ ribbon in the amorphous state. A triangular drive field $H$ with the frequency $f = 5.5$ Hz and the amplitude $H_0 = 25$ A/m was used.

decreases a little with $H_p$ ($\Delta H_c/H_{c0} \approx 0.09$ for $H_p = 24$ A/m) whereas the changes of $M_m$ and $C$ with $H_p$ are slight (Fig. 4). Accordingly, throughout the explored range of $H_0$ (hence also $M_m$), the surface pinning of DWs has little influence on the magnetization processes in amorphous FeCuNbSiB ribbons.

After 1 hour annealing at $T_a = 540^\circ$ C, fine structure of nanocrystalline Fe$_3$Si grains with diameters 10–15 nm forms within the residual amorphous phase [18,19]. At that stage, the magnetocrystalline anisotropy is overcome by the exchange in-
teraction between Fe$_3$Si grains, and the magnetoelastic anisotropy vanishes due to cancellation of the negative magnetostriction of the grains and positive magnetostriction of the amorphous phase [18,19] (the sample becomes nonmagnetostrictive). This results in excellent soft magnetic properties of the annealed sample (Fig. 5a). In particular, a drastic reduction of the coercive field, large increase of $M_m$ and large $\mu_{\text{max}}$ ($H_c = 1.3$ A/m, $M_m/M_s \approx 1$ and $\mu_{\text{max}} \sim 10^5$ Tm/A at $H_0 = 100$ A/m, Table 1) all show that strong volume pinning of DWs vanishes and the surface pinning becomes important. Since $M_m/M_s \approx 1$, in the magnetization processes participates almost the whole domain structure, and the participation of SDS shows up in the width of the maximum of $dM/dt$ vs. $H$ curve in Fig. 5b. The variation of $\log H_c$ with $\log(M_m/M_s)$ for the annealed sample (Fig. 2a) is different from that for as-prepared one and shows two distinctly different regimes depending on $M_m/M_s > / < 0.9$. For $M_m/M_s \leq 0.9$, lower slope of $\log H_c$ vs. $\log(M_m/M_s)$ indicates that weaker surface pinning centres affect the magnetizations processes in this region of $M_m$, whereas a rapid increase of $H_c$ with $M_m$ for $M_m/M_s > 0.9$ implies the stronger pinning of DWs. The variation of $M_r$ with $M_m/M_s$ is qualitatively the same as that of $H_c$ and the absence of saturation of $M_r$ at elevated $M_m$ implies that irreversible motion of DWs is the main magnetization mechanism in both regimes ($M_m/M_s >$ or $< 0.9$). Accordingly, we expect that SDS pinning may be relevant throughout the explored range of $M_m$ ($0.2 \leq M_m/M_s \leq 0.96$).

Fig. 5. $M - H$ loops (a) and the corresponding $dM/dt$ vs. $H$ curves (b) for the amorphous (---) and nanocrystalline Fe$_{73.5}$Cu$_1$Nb$_2$Si$_{15.5}$B$_7$ sample (in the absence of the surface field $H_p$ · · ·) and for $H_p = 24$ A/m (——). The inset: variation of the energy loss $E$ with the magnitude of the static surface field $H_p$ for nanocrystalline sample. The measurements were performed with a triangular drive field of an amplitude $H_0 = 100$ A/m and the frequency $f = 5.5$ Hz.
Figure 6 shows the influence of static $H_p$ on the parameters of the $M-H$ loops of nanocrystalline FeCuNbSiB ribbon in the regime of stronger DW pinning centres ($H_0 = 100 \text{ A/m}$, $M_m/M_s = 0.96$). The coercive field $H_c$ increases with $H_p$ for both directions of $J_D$, but its rate of increase is larger for $H_p \leq 5 \text{ A/m}$ than that for $H_p > 5 \text{ A/m}$. This is exactly the variation predicted by Eqs. (5) and (7) for $k > \tan\langle\delta\rangle$. The continuous increase of $H_c$ with $H_p$ indicates that the enhanced surface pinning of DWs dominates the magnetization processes, whereas the appearance of two regimes ((A) and (B) in the model) with different variations of $H_c$ with $H_p$, implies that the strength of pinning of DWs belonging to MDS is different at the opposite surfaces of the sample. The overall broadening of $dM/dt$ vs. $H$ curve at $H_p = 24 \text{ A/m}$ (Fig. 5b) seems to confirm the assumed influence of $H_p$ on the surface domain structure, whereas the shift of sharp maxima towards higher magnetizing fields $H$ reflects the enhanced pinning of DWs belonging to MDS, i.e. the increase of $H_c$ (Fig. 5a).

For $H_p \leq 5 \text{ A/m}$, also the position of the centre of the $M-H$ loop $C$ varies linearly with $H_p$, which corresponds to the regime A in the model (Eqs. (5) and (6)), where $H_c$ increases due to the influence of $H_p$ on the SDS only. Accordingly, $\Delta H_c/\Delta H_p = k$ (Eq. (5)) and from the data in Fig. 6 we estimate $k \approx 0.067$. Slower increase of $H_c$ with $H_p$ for $H_p > 5 \text{ A/m}$ (regime B, Eq. (7)) shows that the enhancement of SDS pinning of DWs overcomes the additional pressure on DWs due to the projection $P$ of $H_p$, i.e. $kH_p > H_p \tan\langle\delta\rangle$ and $\Delta H_c/\Delta H_p = k - \tan\langle\delta\rangle > 0$ results.
From the slopes of $H_c$ vs. $H_p$ variations for $H_p < 5$ A/m and $H_p > 5$ A/m in Fig. 6 we calculate the angle $\langle \delta \rangle \approx 2.5^\circ$. The smallness of angle $\langle \delta \rangle$ explains small direct influence of $H_p$ on depinning of DWs of MDS, hence the increase of $H_c$ with $H_p$ ($k > \tan(\delta)$). From the data in Fig. 6, by using Eqs. (5) and (7), we also calculated the strengths of pinning of DWs (which are responsible for $H_c$ in the absence of $H_p$) at the opposite surfaces of the sample: $H_{su0} = H_{c0} = 1.3$ A/m and $H_{sl0} = 1.6$ A/m. By inserting the data for $H_{su0}$ and $H_{sl0}$ in Eq. (8), we find $C = \pm 0.15$ A/m which agrees quite well with the experimental results for $C$ around $H_p = 5$ A/m (Fig. 6). From the average slope $\Delta C/\Delta H_p$ for $H_p \leq 5$ A/m, we obtained an independent estimate (Eq. (6)) of angle $\langle \delta \rangle \approx 1.5^\circ$. We note however that the experimental values of $C$ are obtained by subtracting two quantities (Eq. (6)) with similar magnitudes which is subject to large errors. Because of this, we consider the agreement between the two values of $\langle \delta \rangle$ quite good. However, for $H_p > 5$ A/m, $C$ does not seem quite constant (as predicted by Eq. (8)) which may indicate that the enhancement of SDS pinning is not quite the same for the two surfaces of the ribbon ($k_a \neq k_1$). This would affect the variations of $C$ and $H_c$ for $H_p > 5$ A/m and may therefore contribute to the difference in the values of $\langle \delta \rangle$ determined from $H_c(H_p)$ and $C(H_p)$ respectively. Small decrease of $M_m$ on increasing $H_p$ ($\Delta M_m/M_m \approx 0.02$ for $H_p = 24$ A/m) is also consistent with the enhancement of SDS pinning on increasing $H_p$ (Fig. 6). In particular, a fraction of the SDS domains with magnetizations locked in the direction of $H_p$ contributes less to the magnetization of the sample along its axis.

It is interesting to note that in spite of the continuous increase of $H_c$ with $H_p$, the hysteresis loss $E$ (the area of the $M$ vs. $H$ loop) for $H_p \geq 5$ A/m continuously decreases with $H_p$ (inset to Fig. 5a). As illustrated in Fig. 5a, for $H_p = 24$ A/m, this occurs because the magnetization processes become almost reversible for $\mu_0 M > 0.5$ T ($|H| > 10$ A/m) which reduces the overall area of the $M$ vs. $H$ loop in respect to that for $H_p = 0$. Therefore, in nanocrystalline FeCuNbSiB ribbons, the SDS pinning enhanced by $H_p$ has detrimental influence on the magnetization processes at lower magnitudes of $H$ (where the magnetization proceeds via irreversible motion of $180^\circ$-DWs separating MDS domains with magnetizations $I$ forming small angles $\langle \delta \rangle$ with ribbon axis), whereas at higher $H$ (hence $M$), $H_p$ makes the magnetization processes almost reversible which results in lower overall hysteresis loss $E$. Accordingly, one expects particularly strong influence of $H_p$ on the $M$ vs. $H$ loops and their parameters in the region of lower $M_m$ magnitudes.

The measurements performed in the region of weaker DW pinning ($M_m/M_s = 0.66$ and $H_{c0} = 0.74$ A/m for $H_0 = 10$ A/m) confirm these expectations (Fig. 7). As seen from Fig. 7, the variations of $H_c$, $M_m$ and $C$ with static $H_p$ are qualitatively the same as those for $H_0 = 100$ A/m ($M_m/M_s = 0.96$) in Fig. 6, which means that also here SDS pinning dominates the magnetization processes. In particular, the coercive field increases with $H_p$ and this increase is faster for $H_p \leq 5$ A/m than that for $H_p > 5$ A/m.

From the experimental $H_c$ vs. $H_p$ variations (Fig. 6) we extract (by the use of Eqs. (5)−(8)) $k = 0.07$ and $\langle \delta \rangle = 2.4^\circ$ which agree well with the corresponding results obtained for $M_m/M_s = 0.96$. Simultaneously, $M_m$ considerably decreases
with $H_p$ and, inspite of a scatter of the data, the variation of $C$ with $H_p$ is similar to that shown in Fig. 6. We note however that the total change of $H_c$ ($\Delta H_c/H_{c0} \approx 1.1$) and $M_m$ ($\Delta M_m/M_m \approx 0.42$) is much larger than that observed for $M_m/M_s = 0.96$ over the same range of $H_p = 24$ A/m (Fig. 6). This confirms particularly strong influence of the SDS pinning on the magnetization processes in the region of lower magnetizing fields.

Next we briefly examine the influence of dynamic surface field on the coercive field and the position of the centre of the $M-H$ loop for the same sample and $H_0 = 100$ A/m. Figure 7 shows that both for a suitable phase of $J_A$ (Fig. 1) and an unsuitable one, $H_c$ increases with $H_{p0}$, which lends further support to the assumption of enhanced SDS pinning of DWs in the presence of $H_p$. In particular, the increase of $H_c$ with $H_{p0}$ for the suitable phase of $J_A$ is approximately linear in accord with Eq. (13) and the data yield $\Delta H_c/\Delta H_{p0} = k - \tan(\delta) = 0.062$. For the unsuitable phase of $J_A$, the variation of $H_c$ with $H_{p0}$ shows two different regimes (due to $H_{s0} < H_{su0}$) depending on the magnitude of $H_{p0}$: (i) for $H_{p0} \leq 5$ A/m, $H_c$ increases rapidly with $H_{p0}$ and applying Eq. (14) to the data in Fig. 8 we find $\Delta H_c/\Delta H_{p0} = k + \tan(\delta) = 0.11$, (ii) for $H_{p0} > 5$ A/m, the increase of $H_c$ with $H_{p0}$ is slower and the interpretation of the experimental data in terms of Eq. (15) yields $\Delta H_c/\Delta H_{p0} = k - \tan(\delta) = 0.034$.

From the results for unsuitable phase of $J_A$, we obtain $k = 0.072$ and $\langle \delta \rangle = 2.2^\circ$, whereas from the combination of the results for suitable and unsuitable phase of
For $H_{p0} \leq 5$ A/m, $k = 0.068$ and $\langle \delta \rangle = 2.4^\circ$ is found. Therefore, the influence of dynamic $H_p$ (for both phases of $J_A$) on $H_c$ is also consistent with the model (Eqs. (13) – (15)) and yields the same parameters $k$ and $\langle \delta \rangle$ as those calculated from the effects of static $H_p$ on $H_c$ and $C$ of the same sample. The centre of the $M-H$ loop is not influenced by $H_{p0}$ ($C \approx 0$, Fig. 8) which is also consistent with the model.

![Graph](image)

**Fig. 8.** Variation of the coercive field $H_c$ with the amplitude of the dynamic surface field $H_{p0}$, for the suitable phase (■) and unsuitable phase (□) of $H_p$ (see text). (●) represent the corresponding variation of the position of the centre of the $M-H$ loop $C$ for the suitable phase. The triangular magnetizing field with the amplitude $H_0 = 100$ A/m and the frequency $f = 5.5$ Hz was used.

5. **Conclusions**

The influence of static and dynamic surface fields $H_p$ (generated by the core currents) on the parameters ($H_c$, $M_m$) of the $M-H$ loops of optimally annealed FeCuNbSiB ribbons is distinctly different from that which is commonly observed for amorphous soft ferromagnetic ribbons (including the FeCuNbSiB ribbon in the amorphous state). In particular, for nanocrystalline FeCuNbSiB ribbons, $H_c$ continuously increases with $H_p$, whereas for other soft magnetic ribbons it decreases with $H_p$ [3]. We propose that this phenomenon occurs due to strong interplay of the main (inner) domain structure (MDS) and surface domain structure (SDS). More precisely, the pinning of DWs belonging to MDS due to surface domains (SDS pinning [15]) is enhanced in the presence of $H_p$ (which tends to fix and/or rotate the magnetization of SDS domains forming large angles with ribbon axis). This enhanced SDS pinning becomes the dominant mechanism for pinning of DWs in the...
soft ferromagnetic ribbons exhibiting very low intrinsic pinning. Accordingly, we developed a simple model which includes the influence of SDS pinning on the magnetization of the ribbon under simultaneous influence of the magnetizing field \( H \) and \( H_p \). Detailed analysis of the influence of static and dynamic \( H_p \) on \( H_c \), \( M_m \) and \( C \) of nanocrystalline FeCuNbSiB ribbon for two different amplitudes of \( H \) (\( H_0 = 10 \) A/m and 100 A/m, respectively), hence in different regions of \( M_m \), agrees very well with the model predictions. In particular, the analysis shows that the enhancement of SDS pinning of DWs due to \( H_p \) overcomes the direct influence of \( H_p \) (i.e. of its projection \( P = H_p \sin(\langle \delta \rangle) \)) on the DWs belonging to MDS, hence the increase of \( H_c \) with \( H_p \). Although the enhancement of the SDS pinning by \( H_p \) should be a quite general phenomenon for ferromagnetic ribbons, its effects become apparent only when the intrinsic pinning of DWs is very weak and the magnetizations of the MDS domains form very small angles \( \langle \delta \rangle \) with the ribbon axis. Indeed, the preliminary measurements [7] of the influence of \( H_p \) on the magnetization processes in amorphous VITROVC 6026Z ribbon (which has similar domain structure and intrinsic pinning as nanocrystalline FeCuNbSiB ribbons) show that the effects of \( H_p \) on the parameters of the \( M - H \) loop are similar to those described in this article. The above findings are important for the correct evaluation of the performance of such materials in the situations in which they are exposed to external fields with complex configurations. In particular, the unfavourable field configuration (similar to that in this work) can seriously deteriorate their soft magnetic properties even at low amplitudes of the external field.

We wish to emphasize that the proposed model, in addition to providing an insight into the nature and mechanism of DW pinning in soft ferromagnetic ribbons, also allows a quantitative determination of the important characteristic of these materials such as the strength of intrinsic DW pinning \( (H_{sa0}, H_{sb0}) \), the pinning inhomogeneity \( (H_{sa0} > H_{sb0}) \) and the magnetization anisotropy \( (\langle \delta \rangle ) \). The knowledge of these data is necessary in order to select the best methods for the improvement of their magnetic properties. In particular, for the investigated FeCuNbSiB ribbon, the introduction of an uniaxial anisotropy which would increase somewhat the angle \( \langle \delta \rangle \) (for instance by field annealing, or surface treatment [20]) would simultaneously decrease the influence of \( H_p \) on SDS pinning and increase the influence of \( H_p \) on DWs of MDS. More precisely, since \( k \approx 0.07 \) was found for the studied sample, already for the angles \( \langle \delta \rangle \gg 4^\circ \), \( k < \tan(\langle \delta \rangle) \) results and both static and dynamic \( H_p \geq 5 \) A/m should decrease \( H_c \) (Eqs. (7), (13) and (15)).

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References

Proučavali smo utjecaj površinskih polja $H_p$ (proizvedenih stalnom ili izmjeničnom strujom sredine) na meka magnetska svojstva amorfne i nanokristalinične trake $\text{Fe}_{73.5}\text{Cu}_{1}\text{Nb}_{3}\text{Si}_{15.5}\text{B}_7$. Dok se koercitivno polje $H_c$ u amorfnoj traci smanjuje s $H_p$, u nanokristalnoj traci porast $H_c$ stoji za različita polja $H_p$ (staticko, i dinamičko s različitim fazama u odnosu na magnetizirajuću polje $H$). Nastanak koercitivnog polja pojačanog površinskim poljem $H_p$ u nanokristalnoj traci povezuje se s utjecajem $H_p$ na površinsku i osnovnu (unutarnju) domensku strukturu. Razvili smo model koji uključuje to međudjelovanje i objašnjava sve eksperimentalne rezultate. Raspravljamo moguće nepovoljne utjecaje vanjskih polja slične konfiguracije kao $H_p$ na svojstva tih traka i predlažemo načine spriječavanja tih utjecaja.